Progression in Calculation

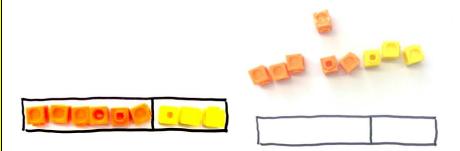
Addition	Subtraction	Multiplication	Division	
Children are encouraged to develop	•	•		
concrete resources including songs and rhymes to develop this process				
Through practical activities they	Through practical activities	Children will experience equal	Children will understand equal	
begin to combine objects and	they begin to understand the	groups of objects.	groups and share items out in	
develop ways of recording	concept of taking objects away		play and problem solving.	
calculations using pictures, photos	and develop ways of recording	They will count in different	They will count in different	
etc.	calculations using pictures,	steps e.g. 2's	steps e.g. 2s	
	photos etc.			
They use numberlines and practical	They use numberlines and			
resources to support calculation and	practical resources to support	They will work on practical		
teachers demonstrate the use of	calculation and teachers	problem solving activities		
the numberline.	demonstrate the use of the	involving equal sets or groups		
	numberline.	involving equal sets of groups		
Bead strings or bead bars can be				
used to illustrate addition.	Bead strings or bead bars can			
	be used to illustrate			
	subtraction.			
000000000	Submachon.			
8+1=9				
	5-1=4			
They will work on practical problem	They will work on practical			
solving activities involving addition.	problem solving activities.			

KS1 Transition

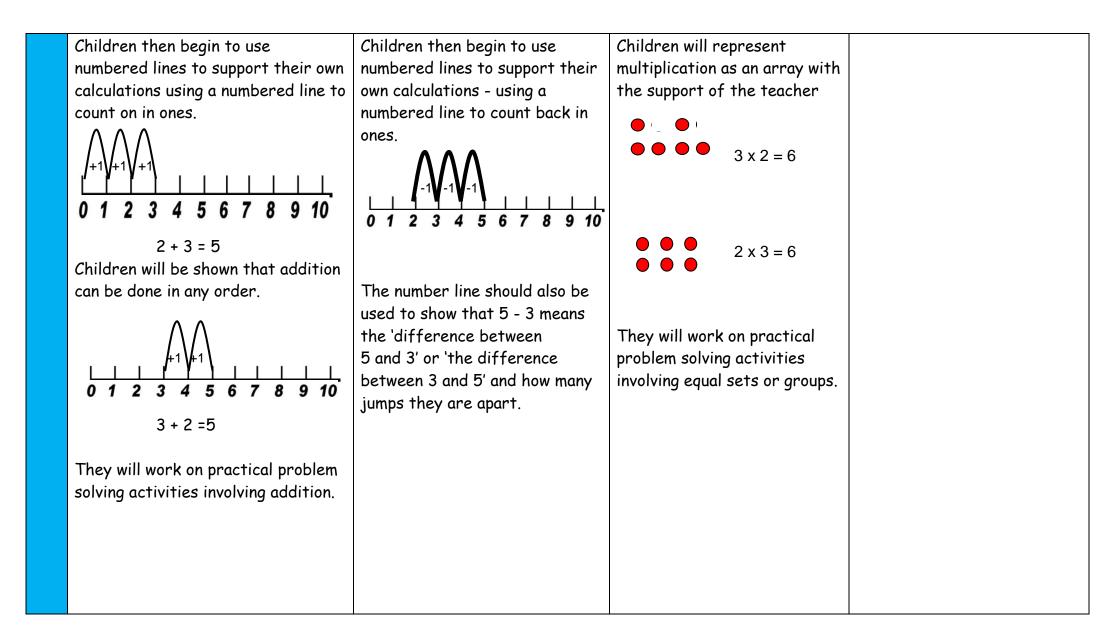
Children will begin to order touch counting to prepare for bar modelling.



If ready, progressing to drawing a bar to show a calculation.



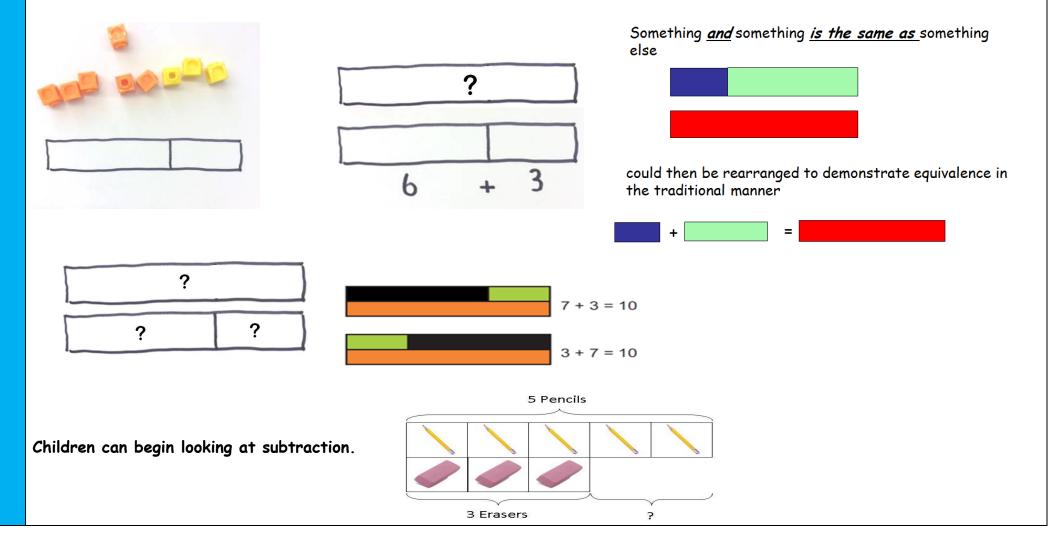
Addition	Subtraction	Multiplication	Division
Through practical activities they combine objects and develop ways of recording calculations using pictures, photos and numbers.	Through practical activities they combine objects and develop ways of recording calculations using pictures, photos and numbers.	Children will experience equal groups of objects. They will count in 2s and 10s and begin to count in 5s.	Children will understand equal groups and share items out in play and problem solving. They will count in 2s and 10s and later in 5s.
Children progress to writing number sentences using pictures and corresponding numerals. $ \begin{bmatrix} \bullet & \bullet \\ \bullet & \bullet \\ \bullet & \bullet \\ \bullet & \bullet \end{bmatrix} = 5 $	Children progress to writing number sentences using jottings and corresponding numerals. 5-3=2	They will begin to understand multiplication as repeated addition and record pictorially, progressing to write the number sentences.	
2 3 Bead strings or bead bars can be used to illustrate addition. 2+3=5	Bead strings or bead bars can be used to illustrate subtraction. 5-3=2	$ \begin{array}{c} \bullet \\ \bullet \\ 2 \\ + \\ 2 \\ + \\ 2 \\ + \\ 2 \\ + \\ 2 \\ + \\ 2 \\ + \\ 2 \\ + \\ 2 \\ + \\ 2 \\ + \\ 2 \\ + \\ 2 \\ + \\ 2 \\ + \\ 2 \\ 2 \\ + \\ - \\ - \\ - \\ - \\ - \\ - \\ - \\ - \\ - \\ -$	



Problem Solving and Reasoning.

This is a mastery curriculum, therefore all children <u>must</u> be reasoning at their level.

Children will continue to use cubes to begin bar modelling but will progress to representing a bar model.



Addition	Subtraction	Multiplication	Division
Children will learn efficient methods to add • 0 + 0 + 0 • TO + 0 • TO + TO Children will use practical equipment to begin using partitioning as a means to adding two 2 digit numbers. Children will use Base 10 and numicon to begin addition through partitioning.	Children will lean efficient methods to subtract • TO - O • TO - TO 24 25 26 27 37 47 Children will use practical equipment to begin using partitioning as a means to subtracting single digit from 2 digit numbers and two 2 digit numbers. Children will use Base 10 and numicon to begin subtracting through partitioning. 25 - 11 = 14	Children will develop their understanding of multiplication and use jottings to support calculation: Repeated addition 24 25 26 27 37 3 times 5 is 5+5+5=15 or $3 \text{ lots of 5} \text{ or } 5 \times 3$ Repeated addition can be shown easily on a number line: $5 \times 3 = 5+5+5$ 45 45 45 45 45 45 45 45	Children will develop their understanding of division and use jottings to support calculation Sharing equally 6 sweets shared between 2 people, how many do they each get? 47 47 47 47 47 47 47 47 47 47 47 47 47

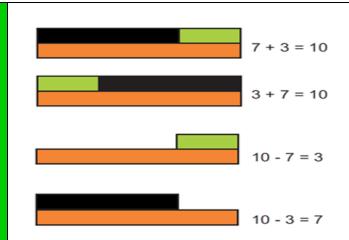
1 T c	They will progress to drawing Base 0 to support mental calculations; $ \circ \circ \qquad \circ \circ$ $32 \qquad + \qquad 21 \qquad = 53$ To support mental strategies, children will become more efficient by adding the tens together first. $32 \qquad + \qquad 21 = 5$	They will progress to drawing Base 10 to support mental calculations; 32 - 11 = 21 To support mental strategies, children will subtract the tens first.	5x3:5+5+5 5 5 566666666	Repeated subtraction using a bead bar 12 ÷ 3 = 4
	30 + 20 = 50 Then adding the ones by using their knowledge of the commutative law	32 - 11 = 30 - 10 = 20 Then subtracting the ones.	0 0 0 0 0 0 0 0 0 3 x 5 = 15	Using symbols to stand for unknown numbers to complete equations using inverse operations
	2 + 1 = 3 or 1 + 2 = 3 50 + 3 = 53	2 - 1 = 1 20 + 1 = 21 32 - 11 = 21	0 0 0 0 0 5 x 3 =15	$\Box \div 2 = 4 \qquad 20 \div \bigtriangleup = 4$ $\Box \div \bigtriangleup = 4$
k	32 + 21 = 53 Children will increase their knowledge of written methods Though the use of column addition.	Children will increase their knowledge of written methods though the use of column	This can also be shown using numicon.	

	subtraction.	
32	45	
+ 34	- 23	
66	22	
They will work on practical problem solving activities involving addition.	They will work on practical problem solving activities involving subtraction.	

Problem Solving and Reasoning.

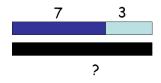
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Children will continue to develop confidence using bar method to represent simple addition calculations. Children will then progress to using bar models to find inverse relationships.



In Year 2, children will be introduced to Cuisenaire rods. They will begin building simple bar models.

With addition & subtraction problems there are three possible <u>unknowns</u> & you can represent them with bars

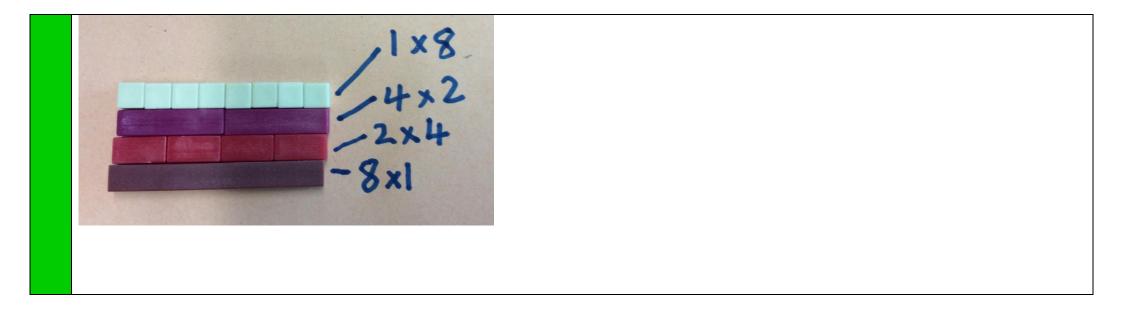


Children will complete simple addition and subtraction problems eg.

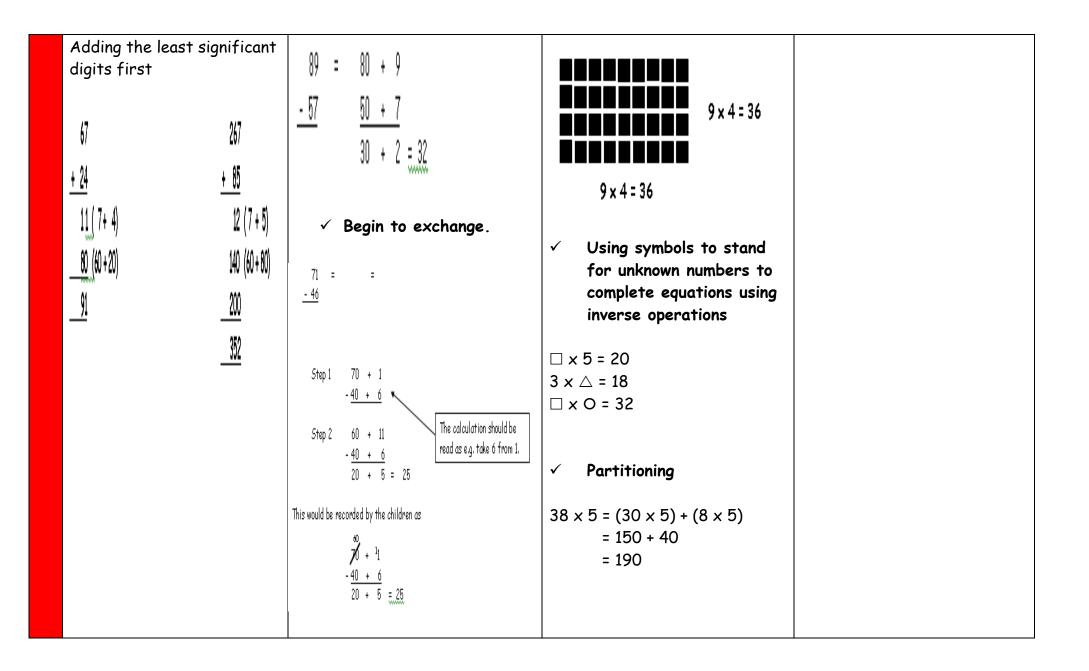
Tom has a bag of 64 marbles. His friend gives him 28 more.

How many does he have now?

Kelsey was running a 26 mile marathon. After 18 miles she felt very tired. How many more miles did she have to run? Children will begin to use Cuisenaire to support multiplication/ division and fraction understanding.



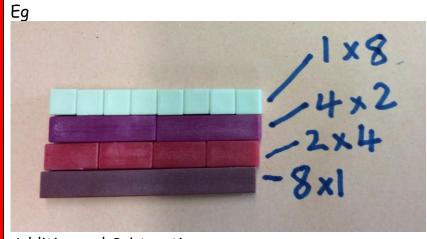
Addition	Subtraction	Multiplication	Division
Children will continue to use	Children will continue to use	Children will continue to use:	Ensure that the emphasis in
informal pencil and paper	informal pencil and paper	 Repeated addition 	Y3 is on grouping and using
methods (jottings) to	methods (jottings).	4 times 6 is 6 + 6 + 6 + 6 =	arrays rather than sharing.
support, record and explain		24 or 4 lots of 6 or 6 x 4	
partial mental methods	✓ Partitioning and		8 ÷ 2 = 4
building on existing mental	decomposition	Children should use bead bars	
strategies.	 Partitioning – demonstrated using arrow cards 	to support their understanding.	$\overline{ \cdot \cdot \cdot }$
Children will continue to	• Decomposition - base 10	6 6 6 6	$\langle \cdot \cdot \cdot \rangle$
draw tens and ones and will	materials		
develop strategies to		000000-0000 00-000000-00 0000	
bridge 10.	NOTE When solving the		Children should also move
	calculation 89 - 57, children		onto calculations involving
	should know that 57 does NOT		remainders using grouping to
	EXIST AS AN AMOUNT it is		support.
	what you are subtracting from the other number. Therefore,	Arrays	13 ÷ 4 = 3 r 1
· · · · · · · · · · · · · · · · · · ·	when using base 10 materials,	Children should be able to	
Making another stick of ten	children would need to count	model a multiplication	✓ Using symbols to stand
from the available ones to	out only the 89.	calculation using an array. This	for unknown numbers to
support bridging ten.		knowledge will support with the	complete equations
		development of the grid	using inverse operations
Children will progress with		method.	
column addition.			26 ÷ 2 = □ 24 ÷ △ =
			12 🗆 ÷ 10 = 8



Problem Solving and Reasoning.

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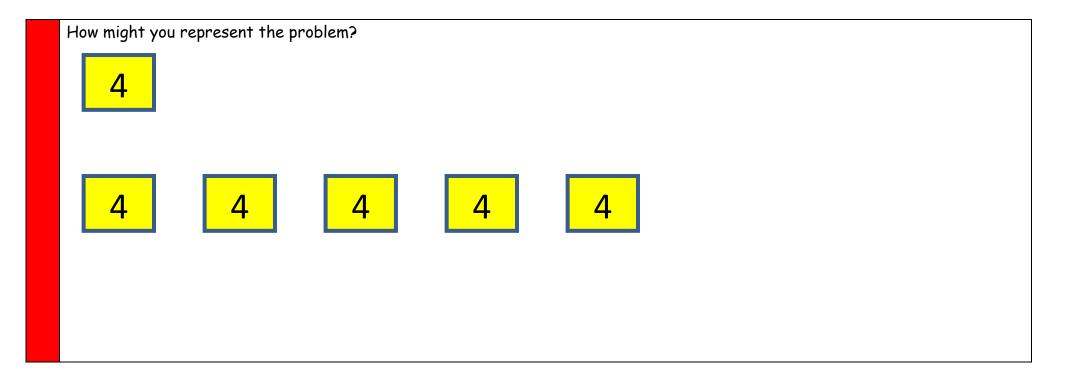
Children will continue to use bar models to support addition/ subtraction/ multiplication and division. Children will continue to use Cuisenaire rods to support alongside drawing their own bar models.

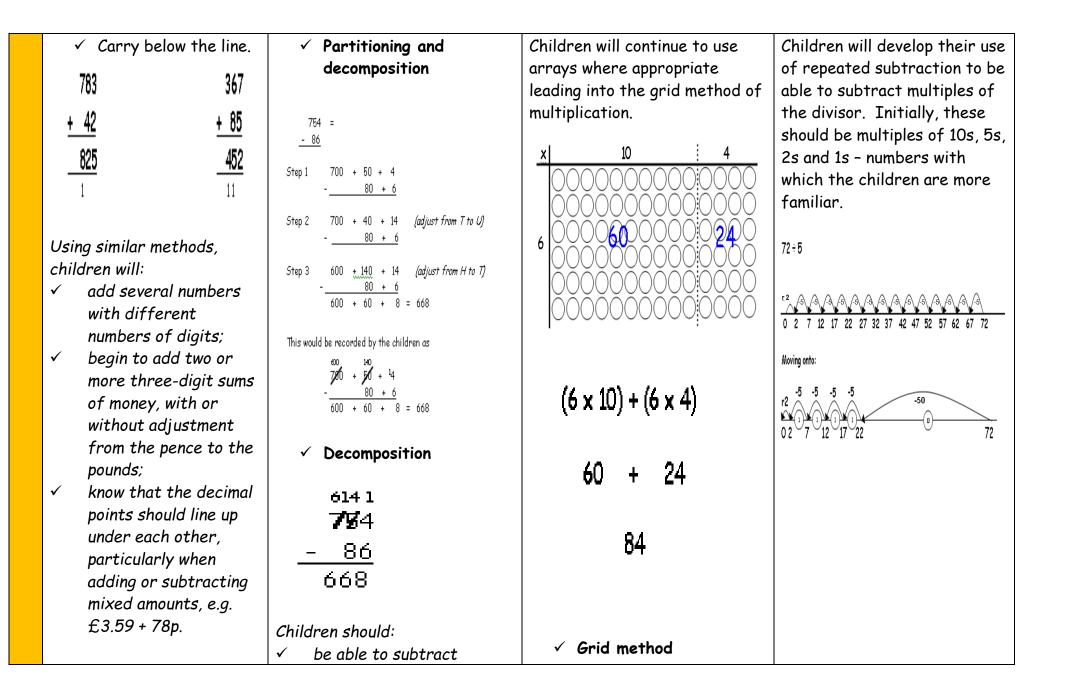


Addition and Subtraction: Carly bought an apple for 17p and a banana for 26p. How much has she spent? Ali had £10. He bought a DVD for £6.70 and a CD for £2.90. How much money did he have left?

Multiplication: Children should begin to use bar models to explain answers and make links between multiplication and division.

Peter has 4 books Harry has five times as many books as Peter. How many books has Harry?





<pre>numbers with different numbers of digits; ✓ using this method, children should also begin to find the difference between two three-digit sums of money, with or without 'adjustment' from the pence to the pounds; ✓ know that decimal points should line up under each other.</pre> <pre> f895 = 8 + 09 + 0.05 leading to -f4.38 = 8 + 0.8 + 0.15 (adjust from Tto U) 8.85 -4 + 0.3 + 0.08 = 64.57 </pre>	TO x O (Short multiplication - multiplication by a single digit) 23 x 8 Children will approximate first 23 x 8 is approximately 25 x 8 = 200 x 20 3 8 160 24 160 $\frac{+ 24}{184}$	Then onto the vertical method: Short division TO \div O 72 \div 3 $3 \overline{) 72} - 30 - 10x - 30 - 10x - 30 - 10x - 30 - 10x - 2x - 30 - 30 - 2x - 30 - 30 - 30 - 30 - 30 - 30 - 30 - 3$
		other multiples.

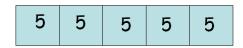
	96 ÷ 6 $ \begin{array}{r} 16 \\ 6) 96 \\ -60 \\ 36 \\ -36 \\ -36 \\ 0 \\ 4nswer : 16 \end{array} $
	Any remainders should be shown as integers, i.e. 14 remainder 2 or 14 r 2.
	Children need to be able to decide what to do after division and round up or down accordingly. They should make sensible decisions about rounding up or down after division.

Problem Solving and Reasoning. This is a mastery curriculum, therefore all children <u>must</u> be reasoning at their level.

Children should build on prior knowledge to use bar models to explain how to find an answer to a problem, focusing on multiplication, division, fractions and percentages.

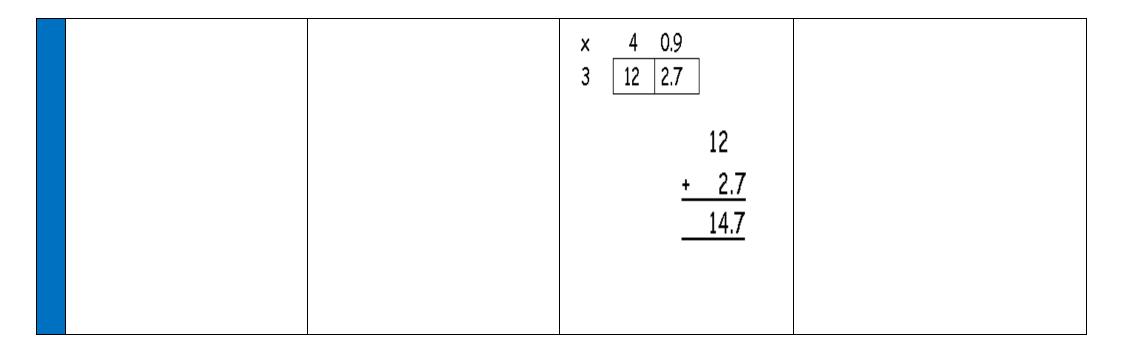
Bob's got a 25 cm bit of wood and saws it into 5 equal pieces. How long's each bit?

Or, in another context, what's 1/5 of 25? (Or 2/5, 3/5 etc)



Addition	Subtraction	Multiplication	Division
Children should extend the	Partitioning and decomposition	Grid method	Children will continue to use written
carrying method to numbers		HTO x O	methods to solve short division TO \div
with at least four digits.	Step 1 754 = 700 + 50 + 4	(Short multiplication –	О.
	этері 794 = 700 + 90 + 4 286200 + 80 + 6	multiplication by a single	
587 3587		digit)	Children can start to subtract larger
+ 475 + 675	Step 2 700 + 40 + 14 <i>(adjust from T to U</i>)	346 × 9	multiples of the divisor, e.g. 30x
	- <u>200 + 80 + 6</u>	Children will approximate	
<u>1062</u> 11		first	Short division HTO ÷ O
11 111	Step 3 600 + 140 + 14 <i>(adjust from H to T)</i>	346 x 9 is approximately 350	
	$-\frac{200 + 80 + 6}{400 + 60 + 8} = 468$	× 10 = 3500	196 ÷ 6
Using similar methods,	100 + 00 + 00 + 00		32 r 4
children will:	This would be recorded by the children as	x 300 40 6	6) 196
✓ add several numbers			- <u>180</u> / 30x
with different numbers	⁶⁰⁰ 7210 + 521 + 4	,	16
of digits;	- <u>200 + 80 + 6</u>	+ 360	
✓ begin to add two or more	400 + 60 + 8 = 468	<u>+ 54</u>	$-\underline{12}$ 4 $2x$
decimal fractions with up	Decomposition	3114	, i i i i i i i i i i i i i i i i i i i
to three digits and the	Decomposition	11	Answer: 32 remainder 4 or 32 r 4
same number of decimal		το × το	
places;	614 1	(Long multiplication –	
 know that decimal points 	784	multiplication by more than a	
should line up under each		single digit)	
other, particularly when	- 286	72 × 38	Any remainders should be shown as
adding or subtracting		Children will approximate	integers, i.e. 14 remainder 2 or 14 r
mixed amounts, e.g. 3.2	468	first	2.
m - 280 cm.	Children should:	72 x 38 is approximately 70	Children need to be able to decide
	✓ be able to subtract	× 40 = 2800	what to do after division and round
			שחמד דס מס מן דפר מועוצוטה מהמ הסטחמ

numbers with different numbers of digits; ✓ begin to find the difference between two decimal fractions with up to three digits and the same number of decimal places; know that decimal points should line up under each other	$\begin{array}{c ccccccccccccccccccccccccccccccccccc$	up or down accordingly. They should make sensible decisions about rounding up or down after division.
	Using similar methods, they will be able to multiply decimals with one decimal place by a single digit number, approximating first. They should know that the decimal points line up under each other. e.g. 4.9 x 3	
	Children will approximate first 4.9 x 3 is approximately 5 x 3 = 15	



Problem Solving and Reasoning. This is a mastery curriculum, therefore all children <u>must</u> be reasoning at their level.

Addition	Subtraction	Multiplication	Division
Children should extend the carrying method to number with any number of digits. 7648 6584 42	Decomposition 5131 Ø467 - <u>2684</u>	ThHTO x O (Short multiplication - multiplication by a single digit) 4346 x 8 Children will approximate first	Children will continue to use written methods to solve short division TO ÷ O and HTO ÷ O. Long division HTO ÷ TO
+ 14% + 5048 6432 9134 12432 7% 111 111 3 + 401 111 3 + 401 111 3 Using similar methods, children will 111 111 ✓ add several numbers with different numbers of digits; ✓ ✓ begin to add two or more decimal fractions with up to four digits and either one or two decimal	 3783 Children should: ✓ be able to subtract numbers with different numbers of digits; ✓ be able to subtract two or more decimal fractions with up to three digits and either one or two decimal places; ✓ know that decimal points should line up under each other. 	4346 × 8 is approximately 4346 × 10 = 43460	972 ÷ 36 $ \begin{array}{c} 27\\ 36 \overline{\smash{\big)}972}\\ -\underline{720}\\ 252\\ -\underline{252}\\ 0\\ 4nswer: 27 \end{array} $ Any remainders should be shown as fractions, i.e. if the children were dividing 32 by 10, the answer should be shown as $3^{2}/_{10}$ which could then be written as $3^{1}/_{5}$ in it's lowest terms.
places; ✓ know that decimal points should line up under each		first 372 x 24 is approximately	Extend to decimals with up to two decimal places. Children should know that decimal points line up under

other, particularly when	400 × 25 = 10000	each other.
adding or subtracting		87.5 ÷ 7
mixed amounts, e.g. 401.2 + 26.85 + 0.71.	$\begin{array}{c ccccccccccccccccccccccccccccccccccc$	$ \begin{array}{c} 12.5 \\ 7) 87.5 \\ - 70.0 \\ 17.5 \\ - 14.0 \\ 3.5 \\ - 3.5 \\ 0 \\ \end{array} $ $ \begin{array}{c} 10 \times \\ 2 \times \\ 0.5 \times \\ 0 \\ \end{array} $ $ \begin{array}{c} Answer : 12.5 \end{array} $
	Using similar methods, they will be able to multiply decimals with up to two decimal places by a single digit number and then two digit numbers, approximating first. They should know that the decimal points line up under each other. For example: 4.92×3 Children will approximate first 4.92×3 is approximately $5 \times 3 = 15$	$ \begin{array}{r} 26 r4 \\ 7) \underline{186} \\ 14 \\ 46 \\ \underline{42} \\ 4 \\ 4 \\ 46 \\ \underline{42} \\ 4 \\ 4 \\ 46 \\ \underline{42} \\ 4 \\ 6 \\ 8 \\ 2 \\ 2 \\ 2 \\ 8 \\ 4 \\ 4 \\ 4 \\ 4 \\ 4 \\ 4 \\ 4 \\ 4 \\ 4 \\ 4 \\ 6 \\ 8 \\ 2 \\ 2 \\ 2 \\ 8 \\ 4 \\ 4 \\ 4 \\ 4 \\ 4 \\ 4 \\ 4 \\ 4 \\ 4 \\ 6 \\ 8 \\ 2 \\ 2 \\ 2 \\ 8 \\ 4 \\ 4 \\ 4 \\ 4 \\ 4 \\ 4 \\ 4 \\ 4 \\ 4 \\ 4 \\ 6 \\ 8 \\ 2 \\ 2 \\ 2 \\ 4 \\ 4 \\ 4 \\ 4 \\ 4 \\ 4 \\ 4 \\ 6 \\ 8 \\ 2 \\ 2 \\ 8 \\ 4 \\ 4 \\ 4 \\ 4 \\ 4 \\ 4 \\ 4 \\ 4 \\ 6 \\ 8 \\ 2 \\ 7 \\ 8 \\ 4 \\ 4 \\ 4 \\ 4 \\ 4 \\ 4 \\ 4 \\ 4 \\ $

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$ \begin{array}{cccccccccccccccccccccccccccccccccccc$	

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By the end of year 6, children will have a range of calculation methods: mental and written. Selection will depend upon the numbers involved. Children should not be allowed to go onto the next stage if:

- They are not ready.
- They are not confident.

Children should be encouraged to **approximate** their answers before calculating.

Children should be encouraged to consider if a mental calculation would be appropriate before using written methods.